Measurements of transverse energy distributions in Au+Au collisions at √sNN = 200 GeV


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Transverse energy \((E_T)\) distributions have been measured for \(Au+Au\) collisions at \(s_{NN}=200\) GeV by the STAR Collaboration at RHIC. \(E_T\) is constructed from its hadronic and electromagnetic components, which have been measured separately. \(E_T\) production for the most central collisions is well described by several theoretical models whose common feature is large energy density achieved early in the fireball evolution. The magnitude and centrality dependence of \(E_T\) per charged particle agrees well with measurements at lower collision energy, indicating that the growth in \(E_T\) for larger collision energy results from the growth in particle production. The electromagnetic fraction of the total \(E_T\) is consistent with a final state dominated by mesons and independent of centrality.

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I. INTRODUCTION

High energy nuclear collisions at the Relativistic Heavy Ion Collider (RHIC) \([1]\) have opened a new domain in the exploration of strongly interacting matter at very high energy density. High temperatures and densities may be generated in the most central (head-on) nuclear collisions, perhaps creating the conditions in which a phase of deconfined quarks and gluons exists \([2,3]\). The fireball produced in such collisions undergoes a complex dynamical evolution, and understanding of the conditions at the hot, dense early phase of the collision requires understanding of the full reaction dynamics.
MEASUREMENTS OF TRANSVERSE ENERGY ...  

Transverse energy $E_T$ is generated by the initial scattering of the partonic constituents of the incoming nuclei and possibly also by reinteractions among the produced partons and hadrons [4,5]. If the fireball of produced quanta breaks apart quickly without significant reinteraction, the observed transverse energy per unit rapidity $dE_T/dy$ will be the same as that generated by the initial scatterings. At the other extreme, if the system reinteracts strongly, achieving local equilibrium early and maintaining it throughout the expansion, $dE_T/dy$ will decrease significantly during the fireball evolution due to the longitudinal work performed by the hydrodynamic pressure [6,7]. This decrease will, however, be moderated by the build-up of transverse hydrodynamic flow, which increases $E_T$ [8]. Finally, gluon saturation in the wave function of the colliding heavy nuclei can delay the onset of hydrodynamic flow, reducing the effective pressure and thereby also reducing the difference between initially generated and observed $E_T$ [9].

$E_T$ production in nuclear collisions has been studied at lower $s$ at the AGS and CERN [10–14] and at RHIC [15]. Within the framework of boost-invariant hydrodynamics [16], these measurements suggest that energy densities have been achieved at the SPS [13] that exceed the deconfinement energy density predicted by lattice QCD [17]. However, from the foregoing discussion it is seen that several competing dynamical effects can contribute to the observed $dE_T/dy$. While the measurement of $E_T$ alone cannot disentangle these effects, a systematic study of $E_T$ together with other global event properties, in particular charged multiplicity and mean transverse momentum $\langle p_T \rangle$, may impose significant constraints on the collision dynamics [8].

In this paper, we report the measurement of $E_T$ distributions from Au+Au collisions at $\sqrt{s_NN}=200$ GeV per nucleon-nucleon pair, measured by the STAR detector at RHIC. $E_T$ is measured using a patch of the STAR Electromagnetic Calorimeter, with acceptance $0<\eta<1$ and $\Delta\phi=60^\circ$, together with the STAR Time Projection Chamber. $E_T$ is separated into its hadronic and electromagnetic components, with the latter dominated by high-$p_T$ photons and $\eta$ decays. The centrality dependence of $E_T$ and $E_T$ per charged particle is studied, and comparisons are made to models and to measurements at lower energy.

A high-temperature deconfined phase could be a significant source of low to intermediate $p_T$ photons [18]. An excess of photons above those expected from hadronic decays has been observed at the SPS for $p_T>1.5$ GeV/c [19]. We investigate this effect through the study of the electromagnetic component of $E_T$.

Section II describes the experimental setup used for the analysis. Section III presents the analysis of the hadronic component of the transverse energy. In Sec. IV, the analysis of the electromagnetic transverse energy is presented. In Sec. V, we discuss the scaling of $E_T$ with the energy of the colliding system and the number of participants $N_{\text{part}}$ and binary collisions $N_{\text{bin}}$ [20], together with theoretical expectations for this scaling. We also discuss the behavior of the electromagnetic component of the transverse energy with the collision energy and centrality. Section VI is a summary and discussion of the main results.

II. STAR EXPERIMENT

This analysis is based on 150 K minimum bias Au+Au collisions measured by the STAR detector in the 2001 RHIC run. STAR [21] is a large acceptance, multipurpose experiment comprising several detector systems inside a large solenoidal magnet. In the following, we describe the detectors which are relevant to the present analysis.

The barrel electromagnetic calorimeter (EMC) [22] is a lead-scintillator sampling electromagnetic calorimeter with equal volumes of lead and scintillator. It has a radius of 2.3 m and is situated just inside the coils of the STAR solenoidal magnet. The electromagnetic energy resolution of the detector is $\delta E/E \approx 16\% / E$ (GeV). The results presented in this work used the first EMC patch installed for the 2001 RHIC run consisting of 12 modules, $\sim 10\%$ of the full planned detector, with coverage $0<\eta<1$ and $\Delta\phi=60^\circ$. Each EMC module is composed of 40 towers (20 towers in $\eta$ by 2 towers in $\phi$) constructed to project to the center of the STAR detector. The transverse dimensions of a tower are approximately $10 \times 10 \text{ cm}^2$, which at the radius of the front face of the detector correspond to a phase space interval of $(\Delta\eta,\Delta\phi)=(0.05,0.05)$. The tower depth is 21 radiation lengths ($X_0$), corresponding to approximately one hadronic interaction length. When fully installed, the complete barrel will consist of 120 modules with pseudorapidity coverage $-1<\eta<1$ and full azimuthal coverage.

The time projection chamber (TPC) [23] has a pseudorapidity coverage of $|\eta|<1.2$ for collisions in the center of STAR, with full azimuthal coverage. In this work, the acceptance of the measurement was limited by the acceptance of the EMC. For charged tracks in the acceptance, the TPC provides up to 45 independent spatial and specific ionization $dE/dx$ measurements. The $dE/dx$ measurement in combination with the momentum measurement determines the particle mass within limited kinematic regions.

The magnetic field was 0.5 T. TPC track quality cuts included z-coordinate (longitudinal axis) selection of the collision vertex within 20 cm of the TPC center and a minimum TPC track space point cut of 10. Typical TPC momentum resolution for the data in this work is characterized by $\delta k/k = 0.0078 + 0.0098 \cdot p_T$ (GeV/c) [23] in which $k$ is the track curvature, proportional to $1/p_T$. Typical resolution of $dE/dx$ measurement is $\sim 8\%$. Additional discussion of TPC analysis is given in the following sections and a more detailed description of the TPC itself can be found in Ref. [23].

The event trigger consisted of the coincidence of signals from the two zero degree calorimeters (ZDC) [24], located at $\theta<2$ mrad about the beam downstream of the first accelerator dipole magnet and sensitive to spectator neutrons. These calorimeters provide a minimum bias trigger which, after collision vertex reconstruction, corresponds to $97 \pm 3\%$ of the geometric cross section $\sigma_{\text{geom}}^{\text{Au+Au}}$. The events were analyzed in centrality bins based on the charged particle multiplicity in $|\eta|<0.5$.

The procedures used in the analysis provide independent measurement of electromagnetic transverse energy and the transverse energy carried by charged hadrons. This latter quantity, corrected to take into account the contribution of
the long-lived neutral hadrons, is designated the hadronic transverse energy. The hadronic component of the transverse energy is obtained from momentum analyzed tracks in the TPC while the electromagnetic fraction is derived from the electromagnetic calorimeter data corrected for hadronic contamination using TPC tracking. In the following sections, we describe how each of these contributions was analyzed to obtain the total transverse energy $E_T$ measurement.

### III. HADRONIC TRANSVERSE ENERGY ($E_T^{\text{had}}$)

The hadronic transverse energy $E_T^{\text{had}}$ is defined as

$$E_T^{\text{had}} = \sum \text{hadrons} \ E_{\text{track}}(ID,p) \sin \theta,$$

where the sum runs over all hadrons produced in the collision, except $\pi^0$ and $\eta$. $\theta$ is the polar angle relative to the beam axis and the collision vertex position. $E_{\text{track}}$ is the energy associated with the particular track, either total or kinetic, as described above, computed from the measured momentum and particle identity (ID) as described below. The factor $C_i(ID,p)$ is defined as

$$C_i(ID,p) = f_{\text{bg}}(p_T) \frac{1}{\int f_{\text{notID}} \text{eff}(p_T)},$$

which includes the corrections for the uncertainty in the particle ID determination, $f_{\text{notID}}$, momentum dependent tracking efficiency, $\text{eff}(p_T)$, and momentum dependent backgrounds, $f_{\text{bg}}(p_T)$. Next, we describe the corrections included in these two factors.

Particle identification was carried out using the measurements of momentum and truncated mean specific ionization $\langle dE/dx \rangle$ in the TPC. For $p_T<1$ GeV/c, assignment was made to the most probable particle type relative to the Bethe-Bloch expectation. Particles were assumed to be pions if $\langle dE/dx \rangle$ differed from this expectation by more than three standard deviations, or if $p_T>1$ GeV/c. The uncertainty in this procedure was gauged by calculating $E_T^{\text{had}}$ for $p_T<1$ GeV/c both with the correct particle assignments and with all particles assumed to be pions. The ratio of these values for $E_T^{\text{had}}$ is applied as a correction for particles that cannot be identified, yielding an overall correction factor to $E_T^{\text{had}}$ of $f_{\text{notID}} = 0.96\pm0.02$. Because this correction was calculated from low momentum particles, it does not account for the centrality variations in the particle ratios with $p_T>1$ GeV/c [25]. On the other hand, particles at $p_T>1$ GeV/c account for about 20% of the total number of particles. Taking into account the centrality-dependence increases the $p/\pi$ and $K/\pi$ ratios at higher $p_T$ generates a change in the estimated hadronic $E_T$ on the order of 2%, which is within the systematic error of $f_{\text{notID}}$.

Only tracks with a transverse momentum $p_T>0.15$ GeV/c were accepted because the tracking efficiency drops rapidly below this value. GEANT [26] detector simulations of HIJING [27] events demonstrate that this cut excludes 5% of the total $E_T^{\text{had}}$. A correction $f_{\text{p-cut}}$ for this effect is included in $C_0$. Taking all simulated tracks for $p_T>0.15$ GeV/c and calculating the energy assuming pions in two extreme cases, one with momentum $p=0$ and the other with $p=0.15$ GeV/c, resulted in a variation of 3% in $E_T^{\text{had}}$, which was assigned as the systematic uncertainty due to this correction.

Since only primary charged tracks measured by the TPC are used in this analysis, we need to correct $E_T^{\text{had}}$ to include the contribution from long-lived neutral hadrons, principally $n(\bar{n}), K^0, K^0_L$, and $\Lambda(\bar{\Lambda})$. The correction factor applied to the data, defined as $f_{\text{neutral}}=E_T^{\text{charged}}/\left(E_T^{\text{charged}}+E_T^{\text{neutral}}\right)$, can be estimated using measurements by STAR at 130 GeV [28–32]. We assume, based on HIJING simulations, that $f_{\text{neutral}}$ does not change significantly from 130 GeV to 200 GeV. We assume that the shape and yield for $K^0$ are the same as for $K^0_L$. The same approximation was applied in the case of $n(\bar{n})$, after subtraction of the contribution from $\Lambda$ decays from the measured $\bar{p}$ yield, and the measured STAR $\bar{p}/p$ ratio [28]. Using this procedure we obtained a value of $f_{\text{neutral}}=0.81\pm0.02$. The uncertainty on this correction was estimated from the uncertainties in the measured STAR spectra. A cross check of these correction factors utilizing 200 GeV measurements [33] generates variations well within the assigned systematic uncertainties.

The correction $f_{\text{bg}}(p_T)$ for background, consisting of electrons, weak decays and secondary tracks that are misidentified as primary, depends on the type of the track and is divided into two separate corrections. The first is for the electrons which are misidentified as hadrons. This correction was estimated using the shape of the electron spectrum obtained from HIJING and GEANT simulations and the absolute yield from STAR data in the region where electrons are identified with high purity using the TPC $dE/dx$ measurements (essentially below 300 MeV). The second term is due to weak decays, which have been included in $f_{\text{neutral}}$ and therefore must be excluded from the primary track population to avoid double counting of their energy. In this case, the correction factor was calculated by embedding simulated particles into real events. By comparison between the simulated particles and the reconstructed ones, the fraction of secondary tracks assigned as primary was evaluated. $\Lambda$ and $K^0_S$ were simulated using the experimental yield and spectral shape measured by STAR [31,32].

The TPC reconstruction efficiency, $\text{eff}(p_T)$, was also determined by embedding simulated tracks into real events and
TABLE I. Corrections and systematic uncertainties for hadronic energy $E^\text{had}_{T}$ for the 5% most central collisions. The quadrature sum of all the systematic uncertainties results in a total of 6.1%. The upper part of the table shows the global corrections included in $C_0$ and the bottom part shows track-wise corrections included in $C_1(ID,p)$. In this case, the correction values for $p_T=0.25$ GeV/c and 1.0 GeV/c are shown.

<table>
<thead>
<tr>
<th>Description</th>
<th>Correction</th>
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<tr>
<td>$f_{p_T&gt;\text{cut}}$</td>
<td>0.95±0.03</td>
</tr>
<tr>
<td>$f_{\text{neutral}}$</td>
<td>0.81±0.02</td>
</tr>
<tr>
<td>$f_{\text{notID}}$</td>
<td>0.96±0.02</td>
</tr>
<tr>
<td>$f_{\text{bg}}(p_T)$</td>
<td>0.84±0.02(0.25 GeV/c)</td>
</tr>
<tr>
<td>$\text{eff}(p_T)$</td>
<td>0.70±0.04(0.25 GeV/c)</td>
</tr>
<tr>
<td></td>
<td>0.80±0.04(1.0 GeV/c)</td>
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</table>

Comparing the simulated input and the final reconstructed event. In order to evaluate the effect of different particle species in the reconstruction efficiency, pions, kaons, and protons were embedded in the real events. In this work, the charged track efficiency correction is the average, weighted by the relative populations of each of these species. The track reconstruction efficiency depends on the transverse momentum of the tracks and the total track density. For central events the efficiency is about 0.7 for tracks with $p_T=0.25$ GeV/c and reaches a plateau at about 0.8 for $p_T>0.4$ GeV/c. This efficiency correction includes the efficiency for track reconstruction, the probability for track splitting, ghost tracks, and dead regions of the TPC.

The resulting systematic uncertainties, taking into account all corrections, combine in quadrature to a systematic uncertainty estimate of 6.1% on $E^\text{had}_{T}$. In Table I we summarize all individual corrections and the corresponding systematic uncertainties.

HIJING and GEANT simulations of $E^\text{had}_{T}$ measured in the acceptance of this study generate event-wise fluctuations of about 10%. Simulations utilizing a substantially larger acceptance (0 < $\eta$ < 1.0 < $\phi$ < 2$\pi$) generate event-wise fluctuations of about 4%, with this latter resolution resulting mainly from tracking efficiency and neutral hadron corrections.

The final $E^\text{had}_{T}$ distribution is corrected for vertex reconstruction efficiency. Peripheral events have lower vertex reconstruction efficiency which suppresses the transverse energy distributions with respect to more central events. The vertex reconstruction efficiency depends on the number of tracks measured in the TPC and varies from 70% to 97%.

IV. ELECTROMAGNETIC TRANSVERSE ENERGY ($E^\text{em}_{T}$)

The electromagnetic transverse energy $E^\text{em}_{T}$ is the sum of the measured transverse energy of electrons, positrons, and photons. The largest fraction of this energy comes from $\pi^0$ decays. Electrons (and positrons) are included because more than 90% of them are produced in the conversion of photons in detector materials. The energy of photons and electrons is fully measured by the calorimeter. There is also a contribution from charged and neutral hadrons produced in the collision that is significant and must be subtracted to permit a measurement of $E^\text{em}_{T}$. In order to remove the hadronic contribution from the measurement, we studied the full spatial profiles of energy deposition by identified hadrons in the EMC. An extensive experimental library of hadronic shower clusters in the calorimeter has been obtained which, in conjunction with TPC tracking, allow a correction for the hadronic background in the calorimeter.

Section IV A discusses the calibration of the EMC using minimum ionizing particles and electrons, while Sec. IV B discusses the correction for hadronic energy deposition in the EMC and Sec. IV C discusses the determination of $E^\text{em}_{T}$.

A. Calibration of EMC

Hadrons striking the EMC deposit a widely fluctuating fraction of their incident energy through hadronic showers. In addition, 30–40% of all high energy charged hadrons penetrate the entire depth of the EMC without hadronic interaction. If such a nonshowering primary charged hadron has sufficient momentum, it will behave like a minimum ionizing particle (MIP) as it transits each of the scintillator layers, resulting in uniform total energy deposition which will be nearly independent of the incident momentum but will vary linearly with the total thickness of the scintillator traversed. Due to the projective nature of the detector, the total length of the scintillator increases with increasing $\eta$. The MIP peak therefore varies from 250 MeV at small $\eta$ to 350 MeV at large $\eta$. The absolute energy of the MIP peak and its $\eta$ dependence was determined from cosmic rays and test beam measurements [34].

The use of MIP particles to calibrate the EMC in situ is convenient and provides a precision tool to track the calibration of the detector over time. In a procedure to minimize systematic uncertainties in the calibration, tracks with $p > 1.25$ GeV/c in the TPC from relatively low multiplicity events are extrapolated to the EMC towers where they are required to be isolated from neighboring charged tracks in a 3 x 3 tower patch ($\Delta \eta \times \Delta \phi = 0.15 \times 0.15$) which has a minimum size of 30 cm x 30 cm ($\eta=0$). Figure 1 shows a typical MIP spectrum measured under these conditions using minimum bias Au+Au events. This example shows the pseudorapidity interval 0.2 < $\eta$ < 0.3. Similar spectra are observed in all $\eta$ bins and provide an absolute calibration in the energy range less than 2 GeV, with an estimated systematic uncertainty of 5% [34].

An absolute calibration over a much wider energy range is obtained using identified electrons tracked with the TPC. This was done by selecting high momentum (1.5 < $p < 5.0$ GeV/c) electrons reconstructed in the TPC. Electron candidates are selected by $dE/dx$ measurement in the TPC. Although the purity of the electron candidates sample in this momentum range is poorer than for low momentum, the hadronic rejection factor obtained from the TPC $dE/dx$ provides a clear electron signal in the calorimeter. Bethe-Bloch predictions for $dE/dx$ of electrons and heavy particles show that the main background in this momentum
FIG. 1. Typical MIP spectrum. x-axis corresponds to ADC channel number. The hits correspond to isolated tracks with \( p > 1.25 \) GeV/c which project to EMC towers. The peak corresponds to the energy deposited by nonshowering hadrons (MIP peak).

range comes from deuterons and heavier particles as well as the tails of the distributions of protons and lower mass particles. In order to minimize systematic uncertainties in this procedure, only tracks having a number of space points greater than 25 were used, as such “long tracks” exhibit better \( dE/dx \) resolution. It was also required that the track should be isolated in a 3\( \times \)3 tower patch in the calorimeter.

As the final electron identifier, the energy, \( E_{\text{tower}} \), deposited in the tower hit by the track is compared to the momentum, \( p \), of the track in the range \( 1.5 < p < 5.0 \) GeV/c. Figure 2 shows the \( p/E_{\text{tower}} \) spectrum for the electron candidates in which it is possible to see a well defined electron peak. The residual hadronic background in this figure can be evaluated by shifting the \( dE/dx \) selection window toward the pion region. The resulting estimate of the hadronic background is shown as a dashed line in the figure. After hadronic background subtraction, the peak position is still not centered at 1 due to the energy leakage to neighboring towers that is not taken into account in this procedure. The amount of leakage depends on the distance to the center of the tower hit by the electron and will shift the peak position to higher values as this distance increases. As shown in Fig. 3, this effect is reproduced well by the full GEANT simulations of the detector response when it is hit by electrons in the momentum range used in this calibration procedure. The upper plot of Fig. 3 shows the position of the electron \( p/E_{\text{tower}} \) peak as a

FIG. 2. \( p/E_{\text{tower}} \) spectrum for electron candidates, selected through \( dE/dx \) from the TPC, with \( 1.5 < p < 5.0 \) GeV/c. A well defined electron peak is observed. The dashed line corresponds to the hadronic background in the \( dE/dx \)-identified electron sample.

FIG. 3. Upper plot: points are measured \( p/E_{\text{tower}} \) electron peak position as a function of the distance to the center of the tower. The solid line is from a calculation based on a full GEANT simulation of the detector response to electrons. Lower plot: points show measured energy deposited by electrons in the tower as a function of the momentum for distances to the center of the tower smaller than 2.0 cm. The first point is the electron equivalent energy of the minimum ionizing particles. The solid line is a second order polynomial fit of the data.
function of this distance. The solid line is a prediction from GEANT simulations. The measurements are in good agreement with the simulations. Figure 3, lower plot, shows the energy deposited in the calorimeter tower as a function of its momentum for electrons in the case where the distance to the center of the tower is smaller than 2.0 cm. (A distance of 5 cm corresponds to the border of a tower at \( \eta = 0 \). The border of the tower at \( \eta = 1 \) is located 7.5 cm from its center.) The first point is the electron equivalent energy of the minimum ionizing particles. A fit to the data using the second-order polynomial of type \( f(x) = a_0 + a_1 x + a_2 x^2 \) is represented by the solid line. The coefficients are \( a_0 = 0.01 \pm 0.08 \text{ GeV} \), \( a_1 = 0.98 \pm 0.11 \text{ c} \), and \( a_2 = 0.01 \pm 0.03 \text{(GeV/}c^2) \). The values of \( a_0 \) and \( a_2 \) are consistent with zero within errors. The small magnitude of these errors indicates that the detector response to electrons is very linear up to \( p = 5 \text{ GeV}/c \).

By combining the MIP calibration and the electron calibration of the EMC, we obtain an overall estimated systematic uncertainty of less than 2% on the total energy measured by the calorimeter. The stability of the detector response was evaluated by monitoring the time dependence of the shape of the raw ADC spectra for each tower, which is the tower response for all particles that reach the calorimeter. In order to have enough statistics, each time interval is larger than one day of data taking but smaller than two days, depending on the beam intensity during that period. The overall gain variation of the detector was less than 5% for the entire RHIC run. The results reported in this paper were obtained from three consecutive days of data taking, in order to minimize any uncorrected effect due to gain variations in the detector.

B. Energy deposited by hadrons in the EMC

As discussed above, for the purposes of measuring electromagnetic energy production it is essential to subtract the hadronic energy deposition in the calorimeter. For charged hadrons, the hit locations on the calorimeter are well determined and if isolated, a cluster of energy is readily identified. In the dense environment of Au+Au collisions, however, it is difficult to uniquely identify the energy deposition associated with a specific hadron track. In this limit, which is relevant for the present measurement, we subtract an average energy deposition based on the measured momentum of the impinging track. Because we are interested in the cumulative distribution averaged over many events and because each event contains many tracks, this averaged correction results in a negligible contribution to the uncertainty in the measured electromagnetic energy.

We have studied hadron shower spatial and energy distributions in the calorimeter both experimentally, using well tracked and identified hadrons in sparse events in STAR, and in detailed GEANT simulations.

A library of separate profiles for pions, kaons, protons, and antiprotons was obtained from GEANT simulations of detector response in the STAR environment (GSTAR). The input events had a uniform momentum distribution in the range \( 0 < p < 10 \text{ GeV}/c \) and an emission vertex limited by \( z_{\text{vertex}} < 20 \text{ cm} \). The constraint on the longitudinal coordi-

![FIG. 4. Mean values from GEANT simulations of the energy deposited in the EMC by various hadronic species as a function of momentum.](image-url)
The shapes of the profiles is observed, with a small normalization.

The sum over EMC towers corresponds to 0. An overall agreement between the shapes of the profiles is observed, with a small normalization difference (see text).

Function of the distance to the center of a tower. The experimental profiles are well described by the simulation, except for a normalization factor on the order of 20% for 0 < p < 0.5 GeV/c and 5% for p > 0.5 GeV/c, as seen in Fig. 5. After renormalization, all experimental profiles up to momentum p = 2.0 GeV/c are in good agreement with simulation and we therefore use the renormalized simulated profiles to allow smooth interpolation in the data analysis and for extrapolation to allow corrections for higher momentum tracks. However, since the interval p < 2.0 GeV/c contains 98% of all tracks, the magnitude of this extrapolation is small for the $E_T$ measurement.

C. $E_T^{em}$ measurement

The electromagnetic transverse energy is defined as

$$E_T^{em} = \sum_{towers} E_{tower}^{em} \sin(\theta_{tower}),$$

where $E_{tower}^{em}$ is the electromagnetic energy measured in an EMC tower and $\theta_{tower}$ is the polar angle of the center of the tower relative to the beam axis and the collision vertex position. Experimentally, $E_T^{em}$ is given by

$$E_T^{em} = \frac{1}{f_{\text{acc}}} \sum_{towers} (E_{tower} - \Delta E_{tower}^{had}) \sin(\theta_{tower}).$$

The sum over EMC towers corresponds to 0 < $\eta$ < 1 and $\Delta \phi = 60^\circ$. $f_{\text{acc}} = \Delta \phi / 2 \pi$ is the correction for the acceptance, $E_{tower}$ is the energy measured by an EMC tower, and $\Delta E_{tower}^{had}$ is the total correction for each tower to exclude the contribution from hadrons. The $\Delta E_{tower}^{had}$ correction is given by

$$\Delta E_{tower}^{had} = \frac{1}{f_{\text{neutral}} \sum_{\text{tracks}} f_{\text{elec}}(p_T) \text{eff}(p_T)} \Delta E(p, \eta, d),$$

where $\Delta E(p, \eta, d)$ is the energy deposited by a track projected on an EMC tower as a function of its momentum $p$, pseudorapidity $\eta$, and distance $d$ to the center of the tower from the track hit point. $f_{\text{elec}}(p_T)$ is a correction to exclude electrons that are misidentified as hadrons and, therefore, should not be added to $\Delta E_{tower}^{had}$. This correction was estimated using the same procedure described in the previous section to exclude real electrons from the $E_T^{had}$ measurement. $\text{eff}(p_T)$ is the track efficiency, as previously discussed, and $f_{\text{neutral}}$ is the correction to exclude the long-lived neutral hadron contribution. As in the case for $E_T^{had} \cdot f_{\text{neutral}} = \Delta E_{tower}^{charged}/(\Delta E_{tower}^{charged} + \Delta E_{tower}^{neutral})$ was estimated from the published STAR data at 130 GeV [28–31]. In this case, $\Delta E_{tower}^{neutral}$ is defined as the energy deposited by all long-lived neutral hadrons. The correction factor is $f_{\text{neutral}} = 0.86 \pm 0.03$.

The systematic uncertainty due to the track efficiency correction, as previously discussed, is 4%. The hadronic correction for charged tracks, $\Delta E(p, \eta, d)$, is based primarily on measured hadronic shower profiles with GEANT simulations used for interpolation between measurements and extrapolation beyond $p = 2$ GeV/c. The systematic uncertainty for this correction to $E_T^{em}$ is estimated from the observed uncertainties in the calculation of the hadronic profile at points in the shower library where full measurements were made. A 5% systematic uncertainty is consistent with the comparison of the measured and calculated shower profiles after normalization. Different from the hadronic component of transverse energy, there is no correction for $p_T$ cutoff in the hadronic background subtraction in the electromagnetic energy. Such low $p_T$ tracks will not reach the calorimeter because of the strength of the magnetic field and, therefore, will not deposit energy in the detector.

As discussed earlier, the systematic uncertainty due to calibration of the detector is of the order of 2% and clearly this uncertainty contributes directly to the uncertainty in $E_T^{em}$. The systematic uncertainty due to the electron background track correction is negligible (<0.5%).

The cumulative effect of all uncertainties discussed in this section, which are assumed to be uncorrelated, is an overall systematic uncertainty estimate for $E_T^{em}$ of 8.0%. All corrections and the corresponding systematic uncertainties are summarized in Table II.

In order to evaluate the hadronic background subtraction procedure and estimate the event-by-event resolution of the reconstructed electromagnetic energy, we have performed simulations in which we compare the reconstructed $E_T^{em}$ energy and the input from the event generator (HIJING). Figure 6 (upper panel) shows the ratio, event by event, of the reconstructed to the input electromagnetic transverse energy as a function of the raw energy measured by the calorimeter in the same acceptance used in this analysis. The smaller the raw EMC energy, the larger the impact parameter of the collision. The reconstructed energy, on average, is the same as the input from the event generator. Edge effects due to the limited acceptance of the detector were also studied and the
TABLE II. Corrections and systematic uncertainties for $E^\text{em}_T$ for
the 5% most central collisions. The quadrature sum of all systematic uncertainties, including the hadronic shower profiles subtraction $[\Delta E(p, \eta, d)]$ not shown in the table, results in a total systematic uncertainty of 8%. The upper part of the table shows the global correction and the bottom part shows track-wise corrections. In this case, the correction values for $p_T=0.25$ GeV/c and 1.0 GeV/c are shown.

<table>
<thead>
<tr>
<th>Description</th>
<th>Correction</th>
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<td>$f_{\text{neural}}$</td>
<td>0.86±0.03</td>
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<tr>
<td>$f_{\text{elec}}(p_T)$</td>
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<tr>
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</tbody>
</table>

...effect on the reconstructed values, on average, is negligible. The event-by-event resolution, however, improves as the event becomes more central. Figure 6 (lower panel) shows the ratio distribution for the most central events. The solid line is a Gaussian fit, from which we estimate the event-by-event resolution of the reconstructed electromagnetic energy to be 14.5% for central events. The main factors that determine this resolution are the hadronic energy subtraction and the corrections for track efficiency and long-lived neutral hadrons. The effect on the global measurement due to the tower energy resolution, considering the EMC patch available, was estimated to be 0.5%, and that due to calibration fluctuations is 0.5%. The fluctuations due to the hadronic background subtraction procedure alone were estimated to be 12%, strongly dependent on the number of tracks used to correct the energy (for larger acceptances this resolution improves). The final $E^\text{em}_T$ distribution is also corrected for vertex reconstruction efficiency.

V. TOTAL TRANSVERSE ENERGY $E_T$

The sum of $E^\text{had}_T$ and $E^\text{em}_T$ is the total transverse energy $E_T$ of the events. In Fig. 7 we present the $E_T$ distribution for minimum bias events, corrected for vertex reconstruction efficiency mainly in the low $E_T$ region. The scale of the upper horizontal axis corresponds to the $E_T$ measurement for the actual acceptance of $0 < \eta < 1$ and $\Delta \phi = 60^\circ$. The bottom axis is scaled to correspond to the $E_T$ for full azimuthal coverage.

In Fig. 7 we also present the $E_T$ distributions for different centrality bins defined by the percentages of the total cross section, selected on charged multiplicity with $\eta < 0.5$. The centrality bin defined as 0–5% (shaded area in Fig. 7) corresponds to the most central collisions amounting to 5% of the total cross section. The data for these centrality ranges are given in Table III. The centrality bins are determined by the uncorrected number of charged tracks with $\eta < 0.5$ and the number of fit points larger than 10. The phase space overlap between the $E_T$ and centrality measurements is small so that there is negligible correlation between them beyond that due to the collision geometry.

At the low energy edge, the distribution exhibits a peak, corresponding to the most peripheral collisions. For the largest values of $E_T$, the shape of the distribution is determined largely by statistical fluctuations and depends greatly on the experimental acceptance [35]. For larger acceptances, the decrease with increasing $E_T$ is very sharp. For this measurement, the fall off of the distribution at large $E_T$ is strongly dominated by the limited acceptance which, at this point, obscures any possible physics fluctuation. Combining the two contributions (hadronic and electromagnetic energies) to the total transverse energy and properly taking into account the correlated uncertainties, we estimate a combined systematic uncertainty in $E_T$ of 7% and an event-by-event resolution of 17%. We obtained for the 5% most central collisions $\langle dE_T/d\eta \rangle = 621 \pm 1 (\text{stat}) \pm 43 (\text{syst})$ GeV, scaled for full azimuthal acceptance and one unit of pseudorapidity.

The upper panel of Fig. 8 shows $\langle dE_T/d\eta \rangle$ per participant pair $N_{\text{part}}/2$ as a function of $N_{\text{part}}$ (obtained using Monte...
FIG. 7. Total transverse energy for $0 < \eta < 1$. The minimum bias distribution is presented as well as the distributions for the different centrality bins (see Table III). The shaded area corresponds to the 5% most central bin. The main axis scale corresponds to the $E_T$ measured in the detector acceptance and the bottom axis is corrected to represent the extrapolation to full azimuthal acceptance.

Carlo Glauber calculations [20]). Data from Au+Au collisions at $s_{NN}=200$ GeV from this analysis are shown together with similar measurements from Pb+Pb collisions at $s_{NN}=17.2$ GeV from WA98 [14] and Au+Au collisions at 130 GeV from PHENIX [15]. These comparison measurements are at $\eta=0$, whereas the measurement reported here is at $0 < \eta < 1$. The gray bands for all three datasets show the overall systematic uncertainty of the data independent of $N_{\text{part}}$, while the error bars show the quadratic sum of the statistical errors, which are typically negligible, and the systematic uncertainties in $E_T$ and $N_{\text{part}}$ [20], with the latter dominating at low $N_{\text{part}}$.

A model based on final state gluon saturation (EKRT [7]) predicts a decrease in more central nuclear collisions for both the charged particle multiplicity per participant and $E_T$.

TABLE III. $E_T$ and $E_{T}^\text{em}$ as a function of the centrality of the collision. Global normalization uncertainties are indicated in the header of the table. All uncertainties are systematic. Statistical errors are negligible.

<table>
<thead>
<tr>
<th>Centrality (%)</th>
<th>$N_{\text{part}}$</th>
<th>$N_{\text{bin}}$</th>
<th>$E_T$ (GeV) $\pm 4.3%$</th>
<th>$E_T^{\text{em}}$ (GeV) $\pm 4.8%$</th>
<th>$E_T/N_{\text{ch}}$ (GeV) $\pm 5.1%$</th>
<th>$E_T/0.5N_{\text{part}}$ (GeV) $\pm 4.3%$</th>
<th>$E_T^{\text{em}}/E_T$ $\pm 3.4%$</th>
</tr>
</thead>
<tbody>
<tr>
<td>70 - 80</td>
<td>14±4</td>
<td>12±4</td>
<td>17.1±0.9</td>
<td>5.8±0.4</td>
<td>0.69±0.07</td>
<td>2.4±0.6</td>
<td>0.342±0.031</td>
</tr>
<tr>
<td>60 - 70</td>
<td>27±5</td>
<td>29±8</td>
<td>37.6±2.0</td>
<td>13.4±0.9</td>
<td>0.75±0.07</td>
<td>2.8±0.5</td>
<td>0.357±0.022</td>
</tr>
<tr>
<td>50 - 60</td>
<td>47±8</td>
<td>64±14</td>
<td>70±4</td>
<td>25.9±1.7</td>
<td>0.79±0.06</td>
<td>3.0±0.5</td>
<td>0.369±0.020</td>
</tr>
<tr>
<td>40 - 50</td>
<td>76±8</td>
<td>123±22</td>
<td>118±6</td>
<td>43±3</td>
<td>0.82±0.06</td>
<td>3.1±0.4</td>
<td>0.364±0.020</td>
</tr>
<tr>
<td>30 - 40</td>
<td>115±9</td>
<td>220±30</td>
<td>187±10</td>
<td>68±4</td>
<td>0.85±0.06</td>
<td>3.2±0.3</td>
<td>0.362±0.019</td>
</tr>
<tr>
<td>20 - 30</td>
<td>166±9</td>
<td>368±41</td>
<td>279±15</td>
<td>100±6</td>
<td>0.86±0.06</td>
<td>3.31±0.25</td>
<td>0.357±0.019</td>
</tr>
<tr>
<td>10 - 20</td>
<td>234±8</td>
<td>591±52</td>
<td>402±21</td>
<td>143±9</td>
<td>0.86±0.06</td>
<td>3.40±0.22</td>
<td>0.356±0.019</td>
</tr>
<tr>
<td>5 - 10</td>
<td>299±7</td>
<td>828±64</td>
<td>515±28</td>
<td>181±12</td>
<td>0.86±0.06</td>
<td>3.43±0.20</td>
<td>0.351±0.019</td>
</tr>
<tr>
<td>0 - 5</td>
<td>352±3</td>
<td>1051±72</td>
<td>620±33</td>
<td>216±14</td>
<td>0.86±0.06</td>
<td>3.51±0.19</td>
<td>0.348±0.019</td>
</tr>
</tbody>
</table>

FIG. 8. $\langle dE_T/d\eta \rangle_{\eta=0.5}$ per $N_{\text{part}}$ pair vs $N_{\text{part}}$. Upper panel: $N_{\text{part}}$ is obtained from Monte Carlo Glauber calculations. The lines show calculations using the HIJING model [27] (solid), the EKRT saturation model [7] [dotted, Eq. (8)], and the two-component fit (dashed, see text). Results from WA98 [14] and PHENIX [15] are also shown. The gray bands correspond to overall systematic uncertainties, independent of $N_{\text{part}}$. Error bars are the quadrature sum of the errors on the measurements and the uncertainties on $N_{\text{part}}$ calculation. Lower panel: the same data are shown as in the upper panel but using and optical Glauber model calculation for $N_{\text{part}}$. The line shows the same result from EKRT model calculation.
Hydrodynamic work during expansion may reduce the observed $E_T$ relative to the initially generated $E_T$, perhaps by a factor of 3 at RHIC energies [7], though this effect will be offset somewhat by the buildup of transverse radial flow [7,8]. The centrality dependence can be approximated by replacing $A/A_{per}$ in the expression for $dE_T/d\eta$ with $s_{NN}$.

The HIJING model predicts an increase in $dE_T/d\eta$ with centrality [20]. The HIJING model is seen to underestimate the data in this case by a factor of 1.18 obtained from HIJING simulations to convert from $s_{NN}$ to $s_{NN}$. The solid line is the prediction using the EKRT model [7] for central Au + Au collisions. As one can see, the EKRT model overestimates the total transverse energy by 15%.

We have also estimated the spatial energy density produced in the collision using $(E_T)^{1/2}$ reported above, converted from pseudorapidity to rapidity density using the factor of 1.18 discussed above. Based on a scaling solution to the relativistic hydrodynamic equations, Bjorken [16] estimated the spatial energy density of the system in terms of the primordial transverse energy produced in the collision $dE_T/dy$, the transverse system size, $R$, and a formation time $\tau_0$.

**TABLE IV. Two-component model fit results of $dE_T/d\eta=AN_{_{part}}+BN_{_{bin}}$.** The uncertainties in the fit parameters include both the data and the $N_{part}/N_{bin}$ uncertainties.

<table>
<thead>
<tr>
<th></th>
<th>$A$ (GeV)</th>
<th>$B/A$</th>
<th>$(B/A)(N_{bin}/N_{part})$</th>
</tr>
</thead>
<tbody>
<tr>
<td>STAR</td>
<td>1.21±0.21</td>
<td>0.17±0.09</td>
<td>0.55±0.14</td>
</tr>
<tr>
<td>PHENIX</td>
<td>0.83±0.18</td>
<td>0.27±0.15</td>
<td>0.71±0.32</td>
</tr>
<tr>
<td>WA98</td>
<td>0.66±0.16</td>
<td>0.28±0.11</td>
<td>0.59±0.23</td>
</tr>
</tbody>
</table>

$E_T^{s_{NN}=0} = 0.43A^{0.92}(s_{NN})^{0.40}(1 - 0.012 \ln A + 0.061 \ln s_{NN}).$

\[ (8) \]
We assumed $\tau_0=1 \text{ fm}/c$, which is the usual value taken in many analyses at SPS energies. For Au+Au at $s_{NN} =200 \text{ GeV}$ we obtained $v_B=4.9\pm 0.3 \text{ GeV/fm}^3$. The uncertainty includes only the uncertainty on $\langle dE_T/d\eta \rangle$. This energy density is significantly in excess of the energy density $1 \text{ GeV/fm}^3$ predicted by lattice QCD for the transition to a deconfined quark gluon plasma [17]. The estimate is based, however, upon the assumption that local equilibrium has been achieved at $\tau =1 \text{ fm}/c$ and that the system then expands hydrodynamically. Comparison of other RHIC data, in particular elliptic flow, to hydrodynamic calculations [37,38,39] indicates that this picture may indeed be valid.

In order to understand the systematic growth in transverse energy with collision energy shown in Fig. 9, we investigate the centrality dependence of $\langle dE_T/d\eta \rangle/\langle dN_{ch}/d\eta \rangle$, the scaling of transverse energy relative to the number of charged particles produced in the collision. The centrality dependence of this ratio may indicate effects of hydrodynamic flow [8]: if the expansion is isentropic, then $dN_{ch}/d\eta$ will remain constant, whereas $dE_T/d\eta$ will decrease due to the performance of longitudinal work.

Figure 10, upper panel, shows the centrality dependence of $\langle dE_T/d\eta \rangle/\langle dN_{ch}/d\eta \rangle$ from STAR measurements at $s_{NN} =200 \text{ GeV}$, compared to similar measurements at 17 and 130 GeV. Data at all energies fall on a common curve within uncertainties, with modest increase from the most peripheral collisions to $N_{part}=100$, reaching a roughly constant value of $\langle dE_T/d\eta \rangle/\langle dN_{ch}/d\eta \rangle$. Figure 10, lower panel, shows the $\langle p_T \rangle$ for 200 GeV Au+Au collisions measured by STAR [40], showing a dependence on centrality similar to that of the transverse energy per charged particle: modest increase with $N_{part}$ for $N_{part}<100$, with constant value for more central collisions. The systematic behavior of $E_T$, multiplicity, and $\langle p_T \rangle$ is similar, indicating that the growth of $E_T$ is due to increased particle production. Quantitative comparison of theoretical models of particle production with the measured centrality dependences of $\langle dE_T/d\eta \rangle/\langle dN_{ch}/d\eta \rangle$ and $\langle p_T \rangle$ of charged particles will constrain the profile of initial energy deposition and the role of hydrodynamic work during the expansion.

In Fig. 11 we show, for central collisions, that this constant transverse energy production per charged particle is observed down to and including AGS measurements at $s_{NN} =5 \text{ GeV}$. A single value of 800 MeV per charged particle or at most a slow logarithmic increase amounting to $<10\%$ characterizes all measurements within errors over a range in which the $E_T$ per participant grows by a factor of 4. HIJING predicts that $E_T$ per charged particle should increase from SPS to RHIC energies due to the enhancement of minijet production at RHIC. However, the predicted increase is rather small and the systematic uncertainties on the measurement do not provide enough precision to significantly test this assumption.

The procedures adopted in this analysis permit an independent measurement of the electromagnetic and hadronic transverse energy. This allows additional exploration of the collision dynamics and particle production. In Fig. 12 we show the ratio of the electromagnetic to the total energy for the most central events as a function of the energy from lower SPS energies [11,41] to our results at full RHIC energy. The observed electromagnetic fraction of the total transverse energy will be strongly influenced by the baryon to meson ratio. At very high energy it is expected that virtually all the $E_T$ will be carried by mesons and the fraction should approximate 1/3, whereas at low energy, baryon dominance of the transverse energy will result in a much smaller electromagnetic fraction.

While the energy dependence seen in Fig. 12 is presumably dominated by the total meson content of the final state, the centrality dependence may provide additional detail about the reaction mechanisms. The centrality dependence of the electromagnetic fraction of our total measured energy is shown in Fig. 13. An excess photon yield may result from the formation of a long-lived deconfined phase, as suggested in Ref. [42]. The predictions from HIJING simulations are also presented. We observe no significant dependence of the electromagnetic fraction with the collision centrality.

**VI. SUMMARY**

We have reported the measurement of transverse energy $E_T$ within $0<\eta<1$, for centrality-selected Au+Au collis-
FIG. 11. \( \langle dE_T/d\eta \rangle / \langle dN_{ch}/d\eta \rangle \) vs \( s_{NN} \) for central events. The error bar in the STAR point corresponds to the systematic uncertainty. A constant value of 800 MeV per charged particle, within errors, characterizes transverse energy production over this full energy range.

FIG. 12. Energy dependence of the electromagnetic fraction of the transverse energy for a number of systems spanning SPS to RHIC energy for central events.

FIG. 13. Participant number dependence of the electromagnetic fraction of the total transverse energy. The results are consistent with HIJING within errors over the full centrality range.

\( s_{NN} = 200 \text{ GeV} \). For the 5% most central events we measured \( \langle E_T \rangle_{5\%} = 621 \pm 43 \text{ (syst)} \) GeV, corresponding to an increase of \( (24 \pm 7)\% \) with respect to measurements at 130 GeV Au + Au collisions at RHIC [15].

We investigated the energy scaling with the number of participant nucleons and with the number of charged particles produced in the collision. We obtained, for the 5% most central events, \( dE_T/d\eta/(0.5N_{\text{part}}) = 3.51 \pm 0.24 \text{ GeV} \) and \( \langle dE_T/d\eta \rangle / \langle dN_{ch}/d\eta \rangle = 860 \pm 70 \text{ MeV} \), respectively. We also compared the results of this work with measurements from AGS and SPS energies. It was found that the increase in the \( E_T \) production from AGS up to RHIC energies comes mostly from the increase in the particle production. A final state gluon saturation model (EKRT), HIJING, and a simple two-component (hard/soft) model were compared to the data. Although the EKRT model predicts a different centrality behavior of energy production, the uncertainties in the \( N_{\text{part}} \) determination do not allow us to discard this model. The simple two-component ansatz suggests that, despite the large uncertainties, the fraction of energy arising from hard processes which is still visible in the final state does not increase significantly from SPS to RHIC energies.

Other measurements at RHIC and comparison to theoretical calculations suggest that a dense, equilibrated system has been generated in the collision and that it expands as an ideal hydrodynamic fluid. The good agreement between hydrodynamic calculations and measurements of particle-identified inclusive spectra and elliptic flow [38] is consistent with the onset of hydrodynamic evolution at a time \( t_0 < 1 \text{ fm}/c \) after the collision [39]. The strong suppression phenomena observed for high \( p_T \) hadrons [43,44,45] suggest that the system early in its evolution is extremely dense. Estimates based on these measurements yield an initial energy density in the vicinity of 50–100 times cold nuclear matter density. Within the framework of boost-invariant scaling hydrodynamics [16], from the \( E_T \) measurement presented here we estimate an initial energy density of about 5 GeV/fm\(^3\). This should be understood as a lower bound [6,9], due to the strong reduction in the observed relative to the initially produced \( E_T \) from longitudinal hydrodynamic work during the expansion. These three quite different approaches produce rough agreement for the estimated initial energy density, with a value well in excess of that predicted by lattice QCD for the deconfinement phase transition [17].

The method used in this analysis permitted an independent measurement of the electromagnetic and hadronic components of the total energy. The electromagnetic fraction of the transverse energy for the 5% most central events...
obtained in this work is \(\langle dE_T^m/d\eta/\langle dE_T/d\eta\rangle=0.35\pm 0.02\), consistent with a final state dominated by mesons. Some models [42] expect that the formation of a long-lived deconfined phase in central events may increase the yield of direct photon production and, therefore, an increase in the electromagnetic fraction of the transverse energy. We, however, observe that the electromagnetic fraction of the transverse energy is constant, within errors, as a function of centrality. Measurements with larger acceptances would have systematic uncertainties significantly reduced and therefore would be able to show smaller effects that cannot be observed with the precision of the present measurement.

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