Identified hadron spectra at large transverse momentum in $p + p$ and $d + Au$ collisions at $\sqrt{s_{NN}} = 200$ GeV

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production is dominated by hard processes (1).

Keywords:

Abstract

We present the transverse momentum ($p_T$) spectra for identified charged pions, protons and anti-protons from $p + p$ and $d + Au$ collisions at $\sqrt{s_{NN}} = 200$ GeV. The spectra are measured around midrapidity ($|y| < 0.5$) over the range of $0.3 < p_T < 10$ GeV/$c$ with particle identification from the ionization energy loss and its relativistic rise in the time projection chamber and time-of-flight in STAR. The charged pion and proton + anti-proton spectra at high $p_T$ in $p + p$ and $d + Au$ collisions are in good agreement with a phenomenological model (EPOS) and with next-to-leading order perturbative quantum chromodynamic (NLO pQCD) calculations with a specific fragmentation scheme and factorization scale. We found that all proton, anti-proton and charged pion spectra in $p + p$ collisions follow $x_T$-scaling for the momentum range where particle production is dominated by hard processes ($p_T \gtrsim 2$ GeV/$c$). The nuclear modification factor around midrapidity is found to be greater than unity for charged pions and to be even larger for protons at $2 < p_T < 5$ GeV/$c$.

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Keywords: Particle production; Perturbative quantum chromodynamics; Fragmentation function; Cronin effect and $x_T$-scaling

1. Introduction

The study of identified hadron spectra at large transverse momentum ($p_T$) in $p + p$ collisions can be used to test the predictions from perturbative quantum chromodynamics (pQCD) [1]. In the framework of models based on QCD, the inclusive production of single hadrons is described by the convolution of parton distribution functions (PDFs), parton interaction cross-sections and fragmentation functions (FFs). The PDF provide the probability of finding a parton (a quark or a gluon) in a hadron as a function of the fraction of the hadron’s momentum carried by the parton. The FFs [2] give the probability for a hard scattered parton to fragment into a hadron of a given momentum fraction. These are not yet calculable from the first principles and hence are generally obtained from experimental data (e.g., $e^+ + e^-$ collisions). The factorization theorem for cross-sections assumes that FFs are independent of the process in which they have been determined and hence represent a universal property of hadronization. It is therefore possible to make quantitative predictions for other types of collision systems (e.g., $p + p$). Comparisons between experimental data and theory can help to constrain the quark and gluon FFs that are critical to predictions of hadron spectra in $p + p$, $p + A$, and $A + A$ collisions. The simultaneous study of identified hadron $p_T$ spectra in $p + p$ and $d + Au$ collisions may also provide important information on the PDFs [3] of the nucleus.

The identified particle spectra in $p + p$ and $d + Au$ collisions also provide reference spectra for particle production at high $p_T$ in Au + Au collisions. Moreover, studies of identified particle production and their ratios as a function of $p_T$ in high-energy heavy-ion collisions have revealed many unique features in different $p_T$ regions [4–7] and between baryons and mesons [8]. A good description of both identified pion and proton spectra

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in $p + p$ and $d + Au$ collisions at intermediate and high $p_T$ by NLO pQCD will provide a solid ground for models based on jet quenching [9] and quark recombination [6]. These emphasize the need for a systematic study of $p_T$ spectra from $p + p$ and $d + Au$ collisions at the same energy as the nucleus–nucleus collisions.

In this Letter, we present the $p_T$ spectra for identified pions, protons and anti-protons in $p + p$ and $d + Au$ collisions at $\sqrt{s_{NN}} = 200$ GeV as measured by the STAR experiment at RHIC. The results are compared to NLO pQCD calculations and a phenomenological model. We also study the $x_T$-scaling in $p + p$ collisions and the nuclear modification factors in $d + Au$ collisions.

2. Experiment and analysis

The STAR experiment consists of several detectors to measure hadronic and electromagnetic observables spanning a large region of the available phase space at RHIC. The detectors used in the present analysis are the time projection chamber (TPC), the the time-of-flight (TOF) detector, a set of trigger detectors used for obtaining the minimum bias data, and the forward time projection chamber for the collision centrality determination in $d + Au$ collisions. The details of the design and other characteristics of the detectors can be found in Ref. [10].

A total of 8.2 million minimum bias $p + p$ collision events and 11.7 million $d + Au$ collision events have been analyzed for the present study. The data set was collected during the years 2001 and 2003. The details of minimum bias trigger conditions for $p + p$ and $d + Au$ collisions can be found in the Refs. [11,12]. The minimum-bias trigger captured 95% of the 30 barn $d + Au$ inelastic cross-section. The tracking efficiency was determined from a cross study of two sets of trigger detectors: two zero-degree calorimeters (ZDCs) and two beam–beam counters (BBCs). The absolute cross-section is derived from a Monte Carlo glauber calculation. These results are consistent with other recent measurements [13]. The trigger for the minimum bias $p + p$ collisions required a coincidence measurement of the two BBCs covering $3.5 < |\eta| < 5.0$ [14]. This trigger was sensitive to color exchange hadronic and doubly-diffractive events; here, these are labelled “non-singly diffractive (NSD) events”. Using PYTHIA(v6.205) [15] and HERWIG [16], it was determined that the trigger measured 87% of the 30.0 ± 3.5 mb NSD cross-section, which was measured via a vernier scan [17]. The data from TOF are used to obtain the identified hadron spectra for $p_T < 2.5$ GeV/c. The procedure for particle identification in TOF has been described in Ref. [18]. For $p_T > 2.5$ GeV/c, we use data from the TPC. Particle identification at high $p_T$ in the TPC comes from the relativistic rise of the ionization energy loss ($dE/dx$). Details of the method are described in Ref. [19]. At $p_T \geq 3$ GeV/c, the pion $dE/dx$ is about 10–20% higher than that of kaons and protons due to the relativistic rise, resulting in a few standard deviations (1–3$\sigma$) separation between them. Since pions are the dominant component of the hadrons in $p + p$ and $d + Au$ collisions at RHIC, the prominent pion peak in the $dE/dx$ distribution is fit with a Gaussian to extract the pion yield [19]. The proton yield is obtained by integrating the entries ($Y$) in the low part of the $dE/dx$ distribution about $2.5\sigma$ away from the pion $dE/dx$ peak. The integration limits were varied to check the stability of the results. Fig. 1 shows a typical $dE/dx$ distribution normalized by the pion $dE/dx$ at $4.5 < p_T < 5.0$ GeV/c and $|\eta| < 0.5$. The Gaussian distribution used to extract the pion yield and the pion, proton and anti-proton peak positions are also shown in the figure.

The kaon contamination is estimated via either of the equations given below. The uncorrected proton yield is

$$p = \frac{(Y - \beta(h - \pi))}{(\alpha - \beta)}$$

or

$$p = \frac{(Y - \beta K_S^0)}{\alpha},$$

where $\alpha$ and $\beta$ are the proton and kaon efficiencies from the integration described above, derived from the $dE/dx$ calibration, resolution and the Bichsel function [19,20]. In the first case the kaon contamination is estimated through the yields of the inclusive hadrons ($h$) and pions, in case two from known yields from $K_S^0$ measurements [19,21]. The typical values of $\alpha$ for a $dE/dx$ cut slightly away from the proton peak position is 0.4 and the $\beta$ values decrease from 0.2 to 0.08 with $p_T$ in the range $2.5 < p_T < 10$ GeV/c. At high $p_T$, the yields of other stable particles (i.e., electrons and deuterons) are at least two orders of magnitude lower than those of pions, and are negligible in our studies. The two results are consistent where STAR $K_S^0$ measurements are available. The $p_T$-dependence of the reconstruction efficiency, background and the systematic uncertainties for pions, protons and anti-protons for low $p_T$ in $p + p$ and $d + Au$ collisions are described in Ref. [18]. At high $p_T$ ($> 2.5$ GeV/c), the efficiency is almost independent of $p_T$ in both $p + p$ and $d + Au$ collisions. The tracking efficiencies are $\sim 88\%$ and $92\%$ in $p + p$ and $d + Au$ collisions, respectively. The difference in tracking efficiency arises because of worse vertex determination in $p + p$ collisions than $d + Au$ collisions. The background contamination to pion spectra for $p_T > 2.5$ GeV/c, primarily from $K_S^0$ weak decay is es-
timated from PYTHIA/HIJING simulations with full GEANT detector descriptions to be $\sim 4\%$. The charged pion spectra are corrected for efficiency and background effects. The inclusive proton and anti-proton spectra are presented with efficiency corrections and without hyperon feed-down corrections. The integrated $A/p$-ratio is estimated to be $< 25\%$ [18,21]. Additional corrections are applied for primary vertex reconstruction inefficiency as discussed in Refs. [11,12,18]. The momentum resolution is given as $\Delta p_T/p_T = 0.01 + 0.005 p_T/(\text{GeV}/c)$ and has $< 4\%$ effect on the yields at the highest $p_T$ value. The spectra are not corrected for momentum resolution effects, but they are included in the systematic errors.

The total systematic uncertainties associated with pion yields are estimated to be $\lesssim 15\%$. This systematic uncertainty is dominated by the uncertainty in modeling the detector response in the Monte Carlo simulations. Protons from hyperon ($Λ$ and $Σ$) decays away from the primary vertex can be reconstructed as primordial protons at a slightly higher $p_T$ than their true value, but with worse momentum resolution. This results in an uncertainty of the inclusive proton yield of $\sim 2\%$ at $p_T = 3$ GeV/c and $\sim 10\%$ at $p_T = 10$ GeV/c. For proton and anti-proton yields at high $p_T$ an additional systematic error arises from the uncertainties in the determination of the efficiencies, $α$ and $β$, under a specific $dE/dx$ selection for integration. This is due to the uncertainties in the mean $dE/dx$ positions for protons and kaons. The total systematic uncertainty in obtaining the proton and anti-proton yields for $p_T > 2.5$ GeV/c increases with $p_T$ from 12% to 23% (at $p_T = 10$ GeV/c) in both $p + p$ and $d + Au$ collisions. The errors shown in the figures are statistical, and the systematic errors are plotted as shaded bands. In addition, there are overall normalization uncertainties from trigger and luminosity in $p + p$ and $d + Au$ collisions of 14% and 10%, respectively [11]. These errors are not shown.

Fig. 2 shows the invariant yields of charged pions, protons and anti-protons for the $p_T$ range of $0.3 < p_T < 10$ GeV/c in minimum bias $p + p$ collisions and for various centrality classes in $d + Au$ collisions. The yields span over eight orders of magnitude. The minimum bias distributions are fit with a Levy distribution [22] of the form

$$\frac{d^2N}{2\pi p_T dp_T dy} = \frac{B}{(1+(m_T-m_0)/nT)^2},$$

where $m_T = \sqrt{p_T^2 + m_0^2}$ and $m_0$ is the mass of the hadron. The Levy distribution essentially takes a power-law form at higher $p_T$ and has an exponential form at low $p_T$. For the $p$ and $\bar{p}$ spectra, fit with a power-law function gives a worse $\chi^2/n\,df$ compared to the fit with the Levy function. For $d + Au$ collisions the $\chi^2/n\,df$ for the power-law fit to $p$ ($\bar{p}$) spectra is 68.55/20 (86.77/20) and the corresponding value for the fit with the Levy function is 21.19/20 (26.4/20).

3. Nuclear modification factor

The nuclear modification factor ($R_{dAu}$) can be used to study the effects of cold nuclear matter on particle production. It is defined as a ratio of the invariant yields of the produced particles in $d + Au$ collisions to those in $p + p$ collisions scaled by the underlying number of nucleon–nucleon binary collisions.

$$R_{dAu}(p_T) = \frac{d^2N_{dAu}/dy dp_T}{\langle N_{\text{bin}} \rangle \sigma_{pp}^{\text{inel}}/d^2p_T dy dp_T},$$

where $\langle N_{\text{bin}} \rangle$ is the average number of binary nucleon–nucleon (NN) collisions per event, and $\sigma_{pp}^{\text{inel}}/d^2p_T dy dp_T$ is the nuclear overlap function $T_A(b)$ [11,12]. The value of $\sigma_{pp}^{\text{inel}}$ is taken to be 42 mb.

The left panel of Fig. 3 shows $R_{dAu}$ values for charged pions ($\pi^+ + \pi^-)/2$) in minimum bias and 0–20% central collisions at $|y| < 0.5$. The $R_{dAu}$ for 0–20% central collisions are higher than $R_{pAu}$ for minimum bias collisions. The result $R_{dAu} > 1$ indicates a slight enhancement of high $p_T$ charged pion yields in $d + Au$ collisions compared to binary collision scaled charged pion yields in $p + p$ collisions within the measured ($y, p_T$) range. The right panel of Fig. 3 shows the $R_{dAu}$ of baryons ($p + \bar{p}$) for the minimum bias collisions at $|y| < 0.5$. The $R_{dAu}$

![Fig. 2: Midrapidity ($|y| < 0.5$) transverse momentum spectra for charged pions, proton and anti-proton in $p + p$ and $d + Au$ collisions for various event centrality classes. Minimum bias distributions are fit to Levy functions which are shown as dashed curves.](image-url)
from PYTHIA(v6.319) predict somewhat more prominent decreasing trend observed in the data. The independent of exists in production. It is, however, not clear whether the same effect is sensitive to nuclear modification of the PDF from processes such as nuclear shadowing and parton saturation as well as to transverse momentum broadening, energy loss in cold nuclear matter and hadronization through recombination, thereby further constraining the models [23].

4. Particle ratios

The particle ratios at midrapidity as a function of $p_T$ for $p + p$ and $d + Au$ minimum bias collisions are shown in Figs. 4 and 5 respectively. Correlated errors are shown as the shaded bands below the data points. The $\pi^-/\pi^+$-ratio has a value $\sim 1$ and is independent of $p_T$ in both $p + p$ and $d + Au$ collisions. The $\bar{p}/p$-ratio for $p + p$ collisions is also independent of $p_T$ within the range studied and has a value of 0.81 $\pm$ 0.1 at 2.5 $<$ $p_T$ $<$ 6.5 GeV/c. However, in $d + Au$ collisions we observe a clear decrease of $\bar{p}/p$ for $p_T > 6$ GeV/c. In quark fragmentation, the leading hadron is more likely to be a particle rather than an anti-particle, and there is no such preference from a gluon jet. A decrease in the anti-particle/particle ratio with $p_T$ would then indicate a significant quark jet contribution to the baryon production. It is, however, not clear whether the same effect exists in $p + p$ collisions or whether the decrease of $\bar{p}/p$ is due to additional nuclear effects in $d + Au$ collisions. Calculations from PYTHIA(v6.319) predict somewhat more prominent $p_T$-dependence [15].

At RHIC, the $p/\pi^+$ and $\bar{p}/\pi^-$ ratios increase with $p_T$ up to 2 GeV/c and then start to decrease for higher $p_T$ in both $p + p$ and $d + Au$ collisions. The $\bar{p}/\pi^-$-ratio rapidly approaches a value of 0.2, which is between the values in $e^+e^-$ collisions for quark and gluon jets [24,25]. The $p/\pi^+$ and $\bar{p}/\pi^-$ ratios from PYTHIA are constant at high $p_T$ in contrast to a decreasing trend observed in the data. The $p/\pi^+$-ratios in $p + \bar{p}$ collisions are again greater than unity for $p_T > 1.0$ GeV/c and is larger than $R_{dAu}$ for charged pions. The $R_{dAu}$ of pions for $2 < p_T < 5$ GeV/c is 1.24 $\pm$ 0.13 and that for $p + \bar{p}$ is 1.49 $\pm$ 0.17 in minimum bias collisions. Identified hadron $R_{dAu}$ are sensitive to nuclear modification of the PDF from processes such as nuclear shadowing and parton saturation as well as to transverse momentum broadening, energy loss in cold nuclear matter and hadronization through recombination, thereby further constraining the models [23].

$p + p$ collisions compare well with results from lower energy ISR and FNAL fixed target experiments [26,27]. Meanwhile, $\bar{p}/\pi^-$-ratios at high $p_T$ have a strong energy dependence with larger values at higher beam energies. In $d + Au$ collisions the $p/\pi^+$-ratio at high $p_T$ is lower for $p + A$ collisions at FNAL energy than at RHIC.

5. Comparison to NLO pQCD and model calculations

In Fig. 6 we compare $(\pi^+ + \pi^-)/2$ and $(p + \bar{p})/2$ yields in minimum bias $p + p$ and $d + Au$ collisions at midrapidity for high $p_T$ to those from NLO pQCD calculations and the phenomenological parton model (EPOS) [28]. The results from EPOS agree fairly well with our data for charged pions and
proton + anti-proton in \(p + p\) and \(d + Au\) collisions. The NLO pQCD results are based on calculations performed with two sets of FFs, the Kniehl–Kramer–Potter (KKP) [29] and the Albino–Kniehl–Kramer (AKK) set of functions [30]. The factorization scale for all the NLO pQCD calculations shown is for \(\mu = p_T\). The charged pion data for \(p_T > 2\) GeV/c in \(p + p\) collisions are reasonably well described by the NLO pQCD calculations using the KKP set of FFs and lower compared to those with AKK FFs underpredict the measured charged pion yields.

The proton + anti-proton yield at high \(p_T\) in \(p + p\) and \(d + Au\) collisions is much higher than the results from NLO pQCD calculations using the KKP set of FFs and lower compared to calculations using AKK FFs. The relatively better agreement of NLO pQCD calculations with AKK FFs compared to those with KKP FFs for proton + anti-proton yields shows the importance of the flavor-specific measurements in \(e^+ + e^-\) collisions in determining the FFs for baryons. One may further improve the NLO pQCD calculations by an all-order resummation of large logarithmic corrections to the partonic cross-sections [34].

6. Scaling of particle production

The invariant cross-sections of inclusive pion production in high energy \(p + p\) collisions have been found to follow the scaling laws [36]:

\[
E \frac{d^3\sigma}{dp_T^3} = \frac{1}{p_T^n} f(x_T) \quad \text{or} \quad E \frac{d^3\sigma}{dp_T^3} = \frac{1}{\sqrt{s}} g(x_T),
\]

where \(x_T = 2p_T/\sqrt{s}\) and \(f(x_T)\) and \(g(x_T)\) are some functions of \(x_T\). Similar scaling has been observed in \(e^+ + e^-\) collisions, but without the \(1/\sqrt{s}^{m}\) or \(p_T^n\) factor [37]. The value of the power \(n\) ranges from 4 to 8 [38]. In the general scaling form \(\sim 1/p_T^n\), \(n\) depends on the quantum exchanged in the hard scattering. In parton models, it is related to the number of point-like constituents taking an active role in the interaction. The value reaches 8 in the case of a quark–meson scattering by exchanging a quark. With the inclusion of QCD, the scaling law follows as \(\sim 1/\sqrt{x_T^n}\), where \(n\) becomes a function of \(x_T\) and \(\sqrt{s}\). The value of \(n\) depends on the evolution of the structure function and FFs. \(n = 4\) is expected in more basic scattering processes (as in QED) [38,39].

Fig. 7 shows the \(x_T\)-scaling of pions, protons and anti-protons. The value of \(n\) obtained for the scaling with \(\sqrt{s}\) of the invariant cross-section is 6.5 \(\pm\) 0.8. The STAR data covers the range 0.003 \(< x_T <\) 0.1. The data points deviate from the scaling behavior for \(p_T < 2\) GeV/c for pions and protons, which could be interpreted as a transition region from soft to hard processes in the particle production. The deviations start at a higher \(p_T\) for the anti-protons. The available data on pion and proton invariant cross-sections at various center-of-mass energies [26,27,33,35,36,40] for \(p_T > 2\) GeV/c are compiled and fitted using the function \(\frac{1}{p_T^n}(1 - x_T)^m\). The value of \(n\) ranges from 6.0 to 7.3 for \(\sqrt{s}=19\) GeV and 540 GeV, while for \(m\) ranges between 13 and 22. The average value of \(n\) for pions is 6.8 \(\pm\) 0.5 and that for protons and anti-protons is 6.5 \(\pm\) 1.0. The variations in \(n\) and \(m\) values may lead to differences in details of scaling behaviour at different energies when the cross-section is multiplied by \(1/p_T^n\) [41]. This feature is not observed in the scaling shown in Fig. 7 due to the data spanning several orders of magnitude. The inset of Fig. 7 shows the \(m_T\)-scaling at \(p_T < 2\) GeV/c, consistent with possible transition between soft and hard processes at around \(p_T \approx 2\) GeV/c. The \(m_T\)-scaling also indicates that flow effects in \(p + p\) and \(d + Au\) collisions are negligible [4,5]. The presented data suggests that the transition region from soft to hard physics occurs around \(p_T \approx 2\) GeV/c in \(p + p\) collisions.

7. Summary

We have presented transverse momentum spectra for identified charged pions, protons and anti-protons from \(p + p\) and
d + Au collisions at $\sqrt{s_{NN}} = 200$ GeV. The transverse momentum spectra are measured around midrapidity ($|y| < 0.5$) over the range of $0.3 < p_T < 10$ GeV/c with particle identification from the ionization energy loss and its relativistic rise in the time projection chamber, as well as the time-of-flight in STAR. The following conclusions can be drawn from the present study: (a) The nuclear modification factor around flight in STAR. The following conclusions can be drawn from the inset shows the $m_T$-scaling of the invariant yields for charged pions and protons + anti-protons in $p + p$ and $d + Au$ collisions.

Acknowledgements

We would like to thank Simon Albino, Stefan Kretzer and Werner Vogelsang for providing us the NLO pQCD results, Klaus Werner for the EPOS results and J. Raufeisen for useful discussions. We thank the RHIC Operations Group and RCF at BNL, and the NERSC Center at LBNL for their support. This work was supported in part by the HENP Divisions of the Office of Science of the US DOE; the US NSF; the BMBF of Germany; IN2P3, RA, RPL, and EMN of France; EPSRC of the United Kingdom; FAPESP of Brazil; the Russian Ministry of Science and Technology; the Ministry of Education and the NNSFC of China; IRP and GA of the Czech Republic, FOM of the Netherlands, DAE, DST, and CSIR of the Government of India; Swiss NSF; the Polish State Committee for Scientific Research; STAA of Slovakia, and the Korea Sci. & Eng. Foundation.

References